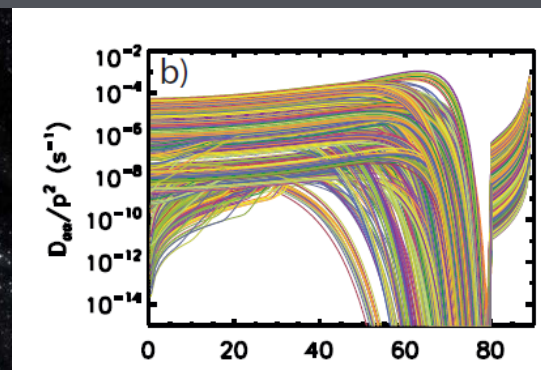
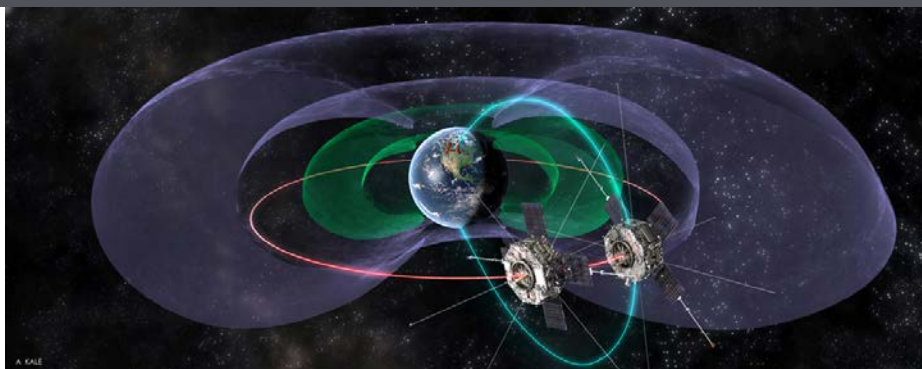
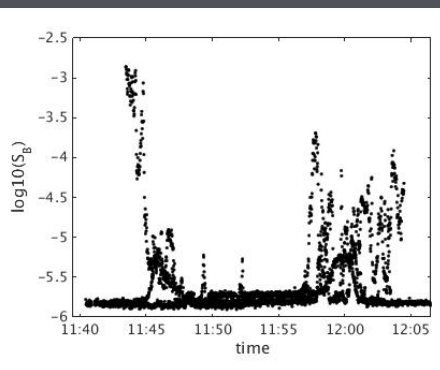


VARIABILITY OF QUASILINEAR DIFFUSION COEFFICIENTS FOR PLASMASPHERIC HISS



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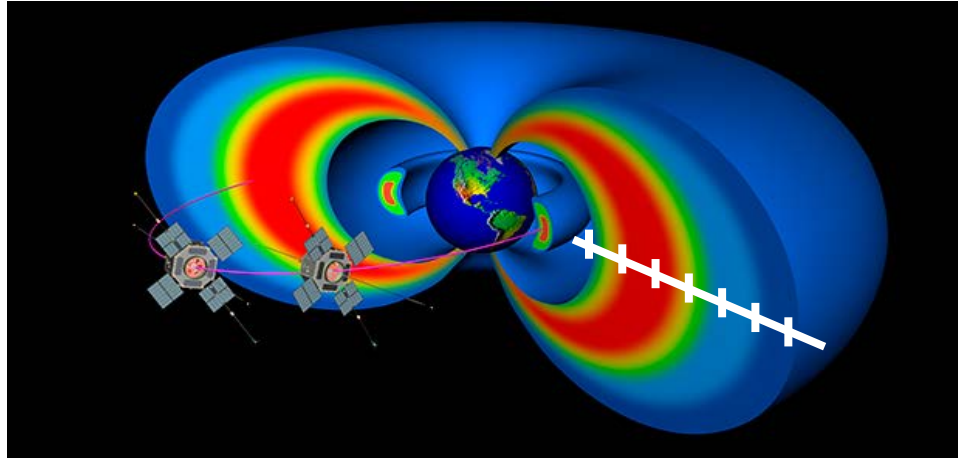
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RADIATION BELT MODELS

- Behaviour of high-energy Radiation Belt electrons controlled in part by wave-particle interactions
- In Radiation Belt Diffusion Models, all physics is “sub grid”
- Wave-particle interactions are captured in diffusion coefficients



MODELLING WAVE-PARTICLE INTERACTIONS

$$D_{\alpha\alpha}(L^*, p, \alpha, t) = \frac{e^2}{4\pi} \sum_n \int_{\theta_{\min}}^{\theta_{\max}} \frac{d\theta}{\cos\theta} \sum_i \frac{\hat{B}_\omega^2(\omega_i, t) G(\theta) |\Phi_{n,k}|^2}{|v_{||} - \partial\omega/\partial k_{||}|_{k_{||,i}}} \left(\frac{\frac{n\Omega_{ce}}{\gamma} - \omega_i \sin^2\alpha}{\cos\alpha} \right)^2$$

wavenormal angle (obs) → θ
 wave amplitude (obs) → $\hat{B}_\omega^2(\omega_i, t)$
 Related to refractive index (requires ω_{pe}/Ω_e , composition - obs) → $|\Phi_{n,k}|^2$
 Range of integral obtained from obs → $\int_{\theta_{\min}}^{\theta_{\max}}$
 Solutions /require ω_{pe}/Ω_e , composition (obs) → $|v_{||} - \partial\omega/\partial k_{||}|_{k_{||,i}}$

- Parameterized models of diffusion coefficients required
 - Drift and bounce averaging required
 - Van Allen Probes will not last forever.

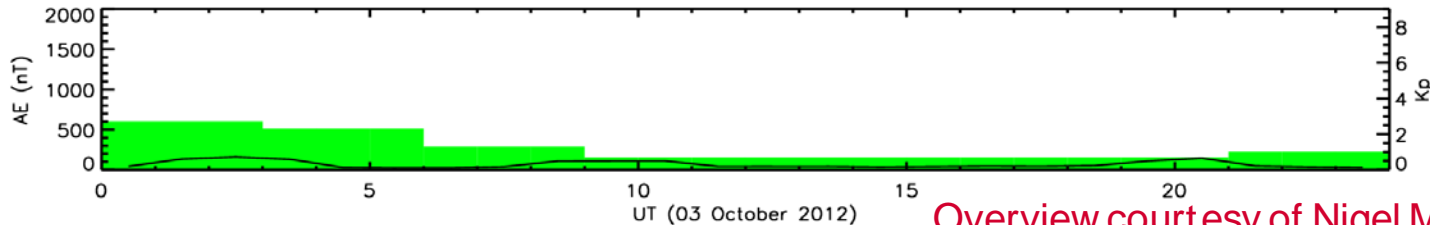
appropriate reference for
Daa

VARIABILITY OF WAVE-PARTICLE INTERACTIONS

Van Allen Probes A, 3rd October 2012

- Large variability of wave properties and ambient plasma properties observed throughout magnetosphere
- Causes of variability

- Data visuals to aid discussion of variability of wave amplitudes



Overview courtesy of Nigel Meredith, BAS



HOW DIFFUSION COEFFICIENTS CAN BE APPLIED IN MODELS

Deterministic methods:

- Parameterize diffusion by e.g. geomagnetic index to capture temporal variation
- One single value of $D_{xy}(L,E,\alpha)$ for each value of parameter
- Run model once for a single event

Stochastic methods:

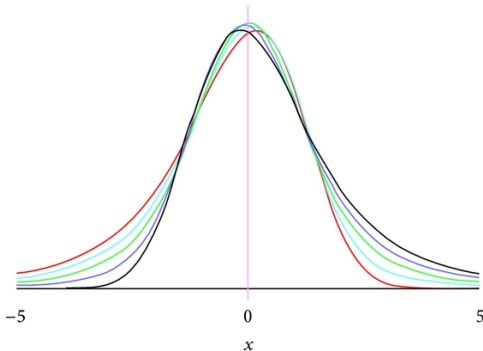
- Construct probabilistic models of diffusion coefficients that include variability
- Run ensembles of diffusion models to obtain realistic range of behaviour*

**Berner et al., BAMS, 2017*

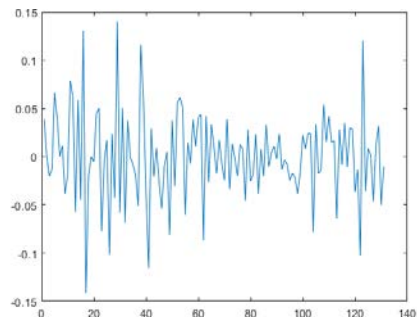


IMPORTANT VARIABILITY DESCRIPTIONS: SEE THOMPSON ET AL POSTER THIS AFTERNOON!

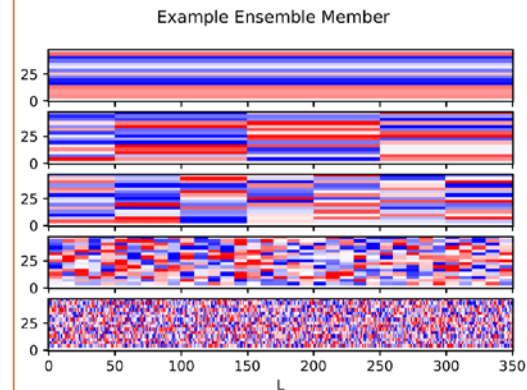
- Underlying distribution



- Temporal scales



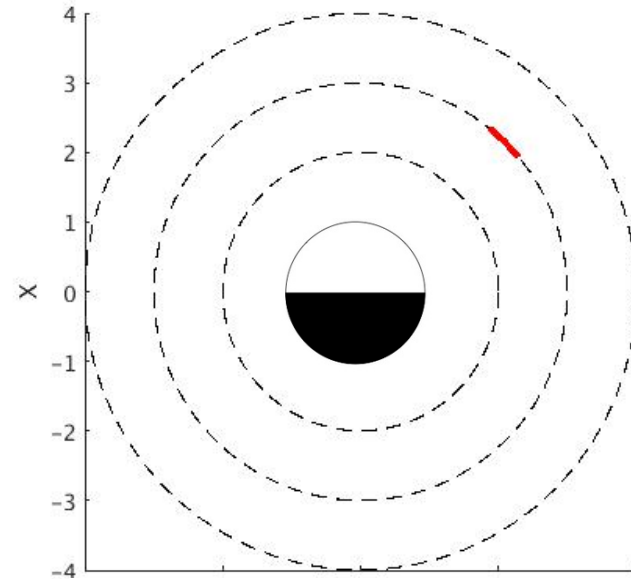
- Spatial scales



Thompson et al, manuscript in preparation

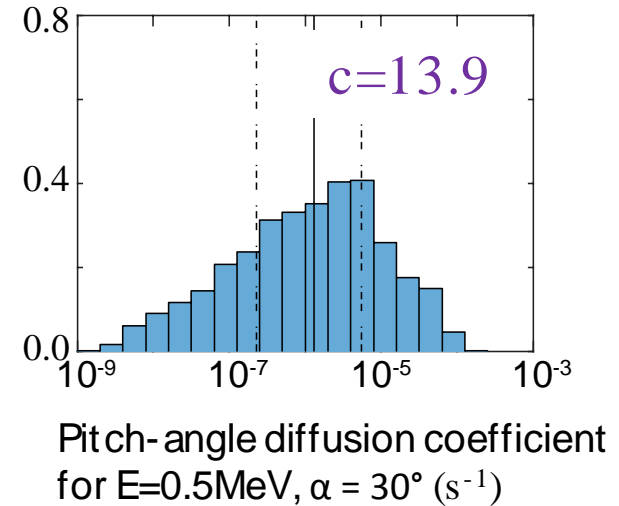
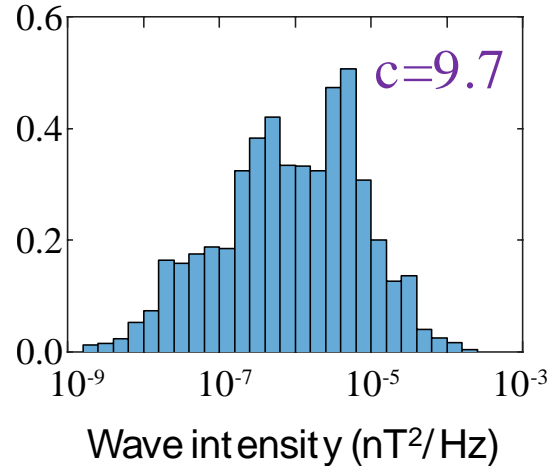
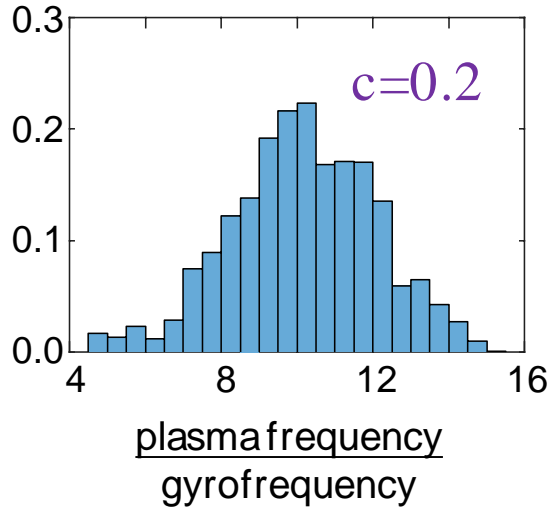
PITCH-ANGLE DIFFUSION FROM PLASMASPHERIC HISS

- Plasmaspheric hiss is near-ubiquitous in high density inner magnetosphere
- Diffusion mainly in pitch-angle
 - Wave characteristics
 - Number density
 - Composition
 - Magnetic field strength
- Van Allen probe A from 2012-2016*
- $9 < \text{MLT} < 10$, $\text{latitude} < 5^\circ$, $2.95 < L^* < 3.05^*$



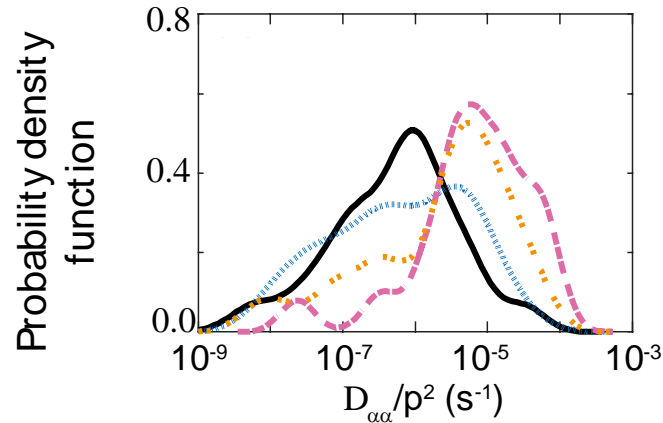
VARIABILITY OF PLASMA, WAVES AND DIFFUSION COEFFICIENT

Probability density function



- Underlying distribution of $D_{\alpha\alpha}$ is log-skew-normal, with large variance
- Coefficient of variance (c , roughly standard deviation/mean or equivalent)
- $c < 1 \rightarrow$ low variance; $c > 1 \rightarrow$ high variance

DIFFUSION COEFFICIENTS SPLIT BY GEOMAGNETIC ACTIVITY



— AE < 50 nT

..... 50 < AE < 100 nT

- - - 100 < AE < 150 nT

- . - . AE > 150 nT

- Would parameterization ever be perfect?
- How much natural variability exists?

CONCLUSIONS

- Variability important for descriptions of wave-particle interactions in magnetosphere
 - See Thompson poster this afternoon
- Diffusion coefficients should be calculated from contemporaneous measurements and we need to know:
 - underlying distribution + variance
 - spatial coherence scales
 - temporal coherence scales
- How “good” can our parameterizations be? Variability may be inevitable.
 - Bentley next for parameterizations of ULF waves